

Are crude Oil, Gas and Coal Prices Cointegrated?

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Abstract

This study examines the existence of long run relation between crude oil, natural gas and coal prices. Energy data for US is used and Based on the result of The Augmented Dickey-Fuller (ADF) tests, autoregressive distributed lag (ARDL) approach is adapted to cointegration analysis. Underlying ARDL model is specified in logarithmic form, so that the coefficients indicate the elasticities. Long run relationship and error correction model (ECM) are estimated for selected ARDL. Moreover, to confirm the stability of the model, CUSUM and CUSUMSQ tests are also conducted with the results that the estimated model is completely stable. The results confirm the existence of long run relation between coal, gas and oil prices. However, in short run gas prices have no effects on the oil prices as its coefficient is insignificant.

Keywords: energy (Oil, Gas, Coal) prices; unit root; cointegration; autoregressive distributed lag (ARDL; ECM model).

1- Introduction

One characteristic of commodity prices is the presence of a unit root in their univariate time series representation, implying that price movements are better characterized as being the sum of permanent and transitory components where the permanent component is a random walk.

However, this study is to examine the long-run relation between crude oil, gas and coal prices. In doing so, tests for unit roots in the univariate time series representation of monthly prices are performed to determine their integration degrees- a prerequisite for the analysis of cointegration. Cointegration is designed to deal explicitly with the analysis of the

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relationship between non-stationary time series. In particular, it allows individual time series to be non-stationary but requires a linear combination of the series to be stationary. Therefore, the basic idea behind cointegration is to search for linear combinations of individually non-stationary time series that are themselves stationary. The methodology used to study common trends in these series is based on the autoregressive distributed lag (ARDL) approach proposed by Pesaran and Shin (Pesaran and Shin, (1995, 1998); Pesaran et al., (1996); Pesaran et al. (2001)).

This paper is developed in six sections. Section two is a short literature review. Section three reports the results of unit root and stationarity tests using Augmented Dickey-Fuller (ADF) approach. Section four describes the methodology of autoregressive distributed lag (ARDL) approach. Section five presents empirical results and the last section reports the main conclusions.

2- Literature Review

What price linkages exist between oil, coal, and natural gas? The main theory here is based on economic substitution. As Bachmeier & Griffin (2006) assert clearly, in the short run coal, oil, and natural gas are not fungible and direct fuel competition is limited. In the long run, these fuels become much closer economic substitutes depending on their respective costs of conversion technologies (Griffin (1979)).

It likes to be probable conjecture that long run relationship between oil, gas and coal price exist. But existence of short run relationship is doubtful.

Serletis (1992) tested for unit roots in the univariate time-series representation of the daily crude oil, heating oil, and unleaded gasoline spot-month future prices. The results showed that the random walk hypothesis for daily energy future prices can be rejected if allowance is made for the possibility of a one-time break in the intercept and the slope of the trend function at an unknown point in time.

Serletis (1994) reported that the maximum likelihood cointegration analysis of daily spot-month crude oil, heating oil and unleaded gasoline future prices covering the period 3 December 1984 to 30 April 1993 led to the conclusion that all three spot-month future prices are driven by only one common trend, suggesting that it is appropriate to model energy future prices as a cointegrated system.

De Vany and Walls (1995) analyzed the degree of integration of the North American gas market and the way price dynamics evolved as these markets were progressively embedded in a larger web of open pipelines and interconnected markets. With the two-step Engle-Granger test for co-integration, spot prices were found to be increasingly co-integrated as open access to the pipelines expands through the network.

King and Cuc (1996) investigated the strength of spot price integration between various natural gas producing basins of North America, from the mid 1980's until the mid 1990's and with time varying parameter (Kalman Filter) and cointegration analysis. Bivariate cointegration tests (Engle-Granger procedure) results were qualitatively similar to De Vany and Walls (1995). Time varying parameter analysis results indicated that price convergence has been emerging in regional markets.

Serletis (1997), in a slightly different manner, tested for shared stochastic trends in the North American markets. Evidence concerning the shared stochastic trends in eight North American natural gas spot markets, using monthly data (1990: 06 - 1996: 01), was obtained by the Engle-Granger approach and the Johansen maximum likelihood approach. Prices within eastern and western areas were found to be driven by different stochastic trends.

Serletis and Herbert (1999) investigated the dynamics of North American natural gas, fuel oil and power prices in the area of eastern Pennsylvania, New Jersey, Maryland and Delaware, using daily data (1996: 10 - 1997: 11) on the Henry Hub and Transco Zone 6 natural gas prices, the PJM (Pennsylvania, New-Jersey and Maryland) power market for electricity price and the fuel oil price for New York Harbor. Correlation between prices in log levels was first investigated and the stationary properties of the prices were analysed using the ADF test. The Engle-Granger Bivariate cointegration test for the pairs of integrated series reported that each pair cointegrates, leading to the conclusion that the same underlying stochastic component affects the three markets.

Asche et al. (2000) investigated the degree of market integration for France, Germany and Belgium. Cointegration tests highlighted that the different border prices for gas to France move proportionally over time and without any significant differences in mean. Furthermore, national markets in Germany, France and Belgium were found to be highly integrated.

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Asche et al. (2002) examined whether the German market was integrated by investigating time series of Norwegian, Dutch and Russian Gas monthly export prices to Germany from January 1990 to December 1997. The Johansen multivariate procedure results showed that gas from the three suppliers compete closely in the same markets since the prices move proportionally over time, but at different price levels.

Hirschhausen et al. (2004) examined the degree of natural gas market integration in Europe, North America and Japan, between the mid 1990's and 2002. Corresponding hypothesis was that there was a certain split of prices between Europe and North America. The relationship between the international gas marker prices and their relation to the oil price, are investigated through principal component analysis and Johansen likelihood-based procedures. Both of them showed a high level of integration within the European/Japanese and North American markets and that the European/Japanese and the North American markets are connected to a much lesser extent.

Warell (2006) tested the hypothesis of the existence of a single economic market for the international coal industry, separated for coking and steam coal, and has investigated market integration over time. This were conducted by applying cointegration and error-correction models on quarterly price series data in Europe and Japan over the time period 1980-2000. Both the coking and the steam coal markets showed evidence of global market integration, as demonstrated by the stable long-run cointegrating relationship between the respective price series in different world regions.

Bachmeier and Griffin (2006) evaluated the degree of market integration both within and between crude oil, coal, and natural gas markets. Their approach yields parameters that can be readily tested against a priori conjectures. Using daily price data for five very different crude oils, they concluded that the world oil market is a single, highly integrated economic market. On the other hand, coal prices at five trading locations across the United States are cointegrated, but the degree of market integration is much weaker, particularly between Western and Eastern coals. Finally, they showed that crude oil, coal, and natural gas markets are only very weakly integrated.

Theodore and Emilie (2007) examined the relationship between UK wholesale gas prices and the Brent oil price over the period 1996–2003 in

order to investigate whether oil and gas prices ‘decoupled’ during this period as orthodox gas market liberalisation theory had suggested. Tests for unit roots and cointegration were carried out and it was discovered that a long-run equilibrium relationship between UK gas and oil prices exists. It was found that the cointegrating relationship is present throughout the sample period. However, the long-run solutions seem to be more volatile. Evidence was provided that the short-run relationship is linear and impulse response functions are used to examine the effects that a shock in oil would have on gas. These findings do not support the assumption that gas prices and oil prices ‘decouple’.

Hammoudeh et al. (2008) examined the dynamic relationship between pairs of four oil benchmark prices (i.e., West Texas Intermediate, Brent, Dubai, and Maya). The results indicated that there is a long-run equilibrium relationship between different benchmarks, regardless of their properties and locations.

3- The Data and Unit Roots

We used data for US energy markets. The Crude Oil Domestic First Purchase Price, the natural gas Wellhead Price and the Cost of Coal Receipts at Electric Generating Plants for coal price were employed. The time period of the analysis extends from October 1983 to October 2008, involving 301 observations¹.

The results of unit roots tests reported by Microfit based on Schwarz Bayesian Criterion (SBC) are as follow:

Table 1: Augmented Dickey-Fuller (ADF) test

variables	an intercept but not a trend		an intercept and a linear trend	
	Critical values	Statistic	Critical values	Statistic
Oil	-2.8714	-2.8683	-3.4264	-3.7656
Gas	-2.8714	-1.5382	-3.4264	-3.6957
Coal	-2.8714	3.0999	-3.4264	3.2806
D1Oil	-2.8718	-5.2030	-3.4270	-5.6448
D1Gas	-2.8718	-5.3603	-3.4270	-5.6208

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D1Coal	-2.8718	1.1232	-3.4270	-.72409
D2Coal	-2.8722	-1.2675	-3.4276	-1.5834
D3Coal	-2.8727	-1.4362	-3.4283	-1.4883
D4Coal	-2.8732	-3.1544	-3.4291	-3.3907
D5Coal	-2.8738	-7.9277	-3.4300	-8.0053

Based on the results of ADF test, oil, gas and coal are integrated processes of degree one, one and five or I (1), I (1) and I (5), respectively.

4- Methodology

There are various techniques for conducting the cointegration analysis. Econometric literature has abundant econometric techniques to investigate cointegration relationships among economic variables. The popular approaches are the well-known residual based approach proposed by Engle and Granger (1987) and the maximum likelihood-based approach proposed by Johansen and Julius (1990) and Johansen (1992).

In applying the cointegration technique, we need to determine the order of integration for each variable. When there are more than two I (1) variables in the system, the maximum likelihood approach of Johansen and Julius has the advantage over residual-based approach of Engle and Granger; however, both of the approaches require that the variables have the same order of integration. This requirement often causes difficulty to the researchers when the system contains the variables with different orders of integration- such as in this study. To overcome this problem, Pesaran et al. (1996, 2001) proposed a new approach known as Autoregressive Distributed Lag (ARDL) for cointegration test that does not require the classification of variables into I(0) or I(1). More recent studies have indicated that the ARDL approach to cointegration is preferable to other conventional cointegration approaches. The ARDL is applicable irrespective of whether the underlying regressors are purely I(0), purely I(1) or mutually cointegrated. The statistic underlying the procedure is the Wald or F-statistic in a generalized Dickey–Fuller type regression, which is used to test the significance of lagged levels of the variables under consideration in a conditional unrestricted equilibrium correction model (ECM) (Pesaran et al, 2001). Besides, ARDL approach is more robust and performs better for small sample sizes than other cointegration techniques.

The ARDL approach involves estimating the conditional error correction version of the ARDL model. The augmented ARDL (p, q_1, q_2, \dots, q_k) is given by the following equation (Pesaran and Pesaran, 1997; Pesaran and Shin, 2001):

$$\alpha(L, p)y_t = \alpha_0 + \sum_{i=1}^k \beta_i(L, q_i)x_{it} + \lambda'w_t + \varepsilon_t \quad \forall t=1, 2, \dots, n \quad (3)$$

Where

$$\alpha(L, p) = 1 - \alpha_1 L - \alpha_2 L^2 - \dots - \alpha_p L^p$$

$$\beta_i(L, q_i) = \beta_{i0} - \beta_{i1}L - \beta_{i2}L^2 - \dots - \beta_{iq_i}L^{q_i} \quad \forall i=1, 2, \dots, k$$

y_t is the dependent variable, α_0 is the constant term, L is the lag operator, w_t is $1 \times s$ vector of deterministic variables such as intercept term, time trends, or exogenous variables with fixed lags. x_t is the k -dimensional forcing variables which are not cointegrated among themselves. ε_t is a vector of stochastic error terms, with zero means and constant variance-covariance.

The long-run coefficients are estimated by:

$$\pi = \frac{\hat{\lambda}(\hat{p}, \hat{q}_1, \hat{q}_2, \dots, \hat{q}_k)}{1 - \hat{\alpha}_1 - \hat{\alpha}_2 - \dots - \hat{\alpha}_{\hat{p}}}$$

where $\hat{\lambda}(\hat{p}, \hat{q}_1, \hat{q}_2, \dots, \hat{q}_k)$ denotes the OLS estimates of λ' in equation (1) for the selected ARDL model.

The error correction model (ECM) related to the ARDL($\hat{p}, \hat{q}_1, \hat{q}_2, \dots, \hat{q}_k$) can be obtained by writing equation (3) in terms of lagged levels and the first difference of $y_t, x_{1t}, x_{2t}, \dots, x_{kt}$ and w_t :

$$\Delta y_t = \Delta \alpha_0 - \alpha(1, \hat{p})ECM_{t-1} + \sum_{i=1}^k \beta_{i0}x_{it} + \lambda' \Delta w_t - \sum_{j=1}^{\hat{p}-1} \alpha_j \Delta y_{t-j} - \sum_{i=1}^k \sum_{j=1}^{\hat{q}_i-1} \beta_{ij} \Delta x_{i,t-j} + \varepsilon_t \quad (5)$$

where ECM is the error correction model and it is defined as follows:

$$ECM_t = y_t - \hat{\alpha} - \sum \hat{\beta}_{i0} x_{it} - \lambda' w_t$$

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The ARDL approach involves two steps for estimating the long-run relationship (Pesaran et al., 2001). The first step is to examine the existence of long-run relationship among all variables in the equations under estimation. The second step is to estimate the long-run and the short-run coefficients of the same equation. We run the second step only if we find a long-run relationship in the first step (Narayan, et al. 2004).

5- Autoregressive Distributed Lag (ARDL) Model and Empirical Results

Because underlying variables (Oil, Gas and Coal) have different integration degrees, ARDL approach is adopted for cointegration analysis.

Our ARDL model to estimate long-run relationship among underlying variables, in logarithmic form, is specified as follows:

$$LOil = \alpha_0 + \alpha t + \sum_{i=1}^{p-1} \beta_i LOil_{t-i} + \sum_{j=0}^{q-1} \theta_j LGas_{t-j} + \sum_{j=0}^{q-1} \theta_{2j} LCoal_{t-j} + \varepsilon_t \quad (7)$$

Where α_0 is the constant term, and t is time trend.

Using Microfit for estimation, ARDL (2, 0, 0) is selected based on Schwarz Bayesian Criterion (SBC). Table (2) shows the results for the selected ARDL model.

**Table 2: Autoregressive Distributed Lag Estimates
ARDL (2,0,0) selected based on Schwarz Bayesian Criterion**

Regressor	Coefficient	T-Ratio	Standard Error
LOil(-1)	1.3854	26.2829	.052712
LOil(-2)	-.48740	-9.1044	.053534
LGas	.039038	1.7886	.021826
LCoal	.021046	3.4231	.061481
Constant	.15225	3.5821	2.3791
Time trend	.32883	3.1119	.10563
R-Squared = .98078		R-Bar-Squared = .98044	
F-statistic F(5, 281) = 2868		Schwarz Bayesian Criterion = 333.9134	

As the table indicates all the statistics of the estimated model, except for gas price coefficient, are satisfactory.

To confirm the stability of the estimated model, the tests of Cumulative Sum of Recursive Residuals (CUSUM) and Cumulative Sum of Squares of Recursive Residuals (CUSUMSQ) are employed in this paper. Figures (1) and (2) provide the graphs of CUSUM and CUSUMSQ tests, respectively.

These figures indicate that the plots of CUSUM and CUSUMQ are completely stable within 5% of critical bands.

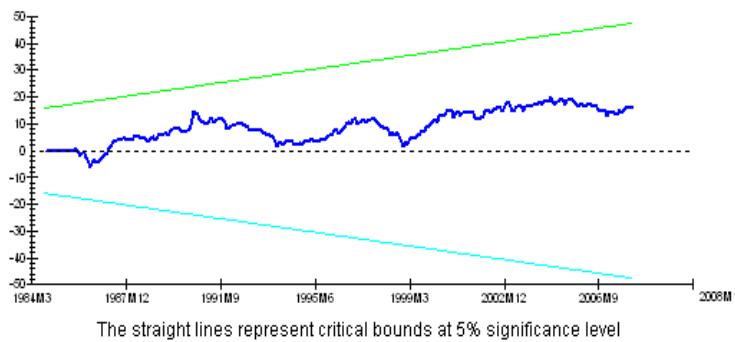


Figure 1: Cumulative Sum of Recursive Residuals (CUSUM)

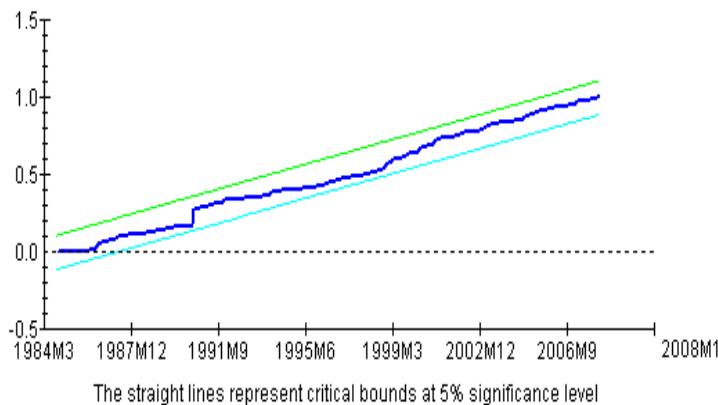


Figure 2: Cumulative Sum of Squares of Recursive Residuals (CUSUMSQ)

The results of estimated long run regression and the corresponding ECM model are reported in tables (3) and (4).

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Table 3: Estimated Long Run Coefficients using the ARDL Approach

ARDL (2, 0, 0) selected based on Schwarz Bayesian Criterion

Regressor	Coefficient	T-Ratio	Standard Error
LGas	.38281	2.2419	.17076
LCoal	2.0638	4.2164	.48946
Constant	1.4930	7.8976	.18904
Time trend	.0032238	2.9587	.0010896

Table (4): Error Correction Representation for the Selected ARDL Model

ARDL (2,0,0) selected based on Schwarz Bayesian Criterion

Regressor	Coefficient	T-Ratio	Standard Error
D2LOil	.48740	9.1044	.053534
D1LGas	.039038	1.7886	.021826
D1LCoil	.21046	3.4231	.061481
DConstant	.15225	3.5821	.042502
DTime trend	.32883	3.1119	.10563
ECM(-1)	-.10198	-4.4794	.022765
R-Squared = .25578		R-Bar-Squared = .24254	
F-statistic F(5, 281) 19.3156		Schwarz Bayesian Criterion = 333.9134	

As table (3) indicates, the coefficients (Gas prices and Coal prices) are statistically significant.

From table (4), it is clear that the error correction term (ECM (-1)) has the right sign (negative) and is statistically significant. Specifically, the estimated value of EC_{t-1} is -.10198.

The absolute value of the coefficient of EC_{t-1}, indicating the speed of adjustment to equilibrium, denotes that 10% of any shocks dumps out in each period, converging back to the long run equilibrium. Bannerjee, Dolado and Mestre (1998), hold that a highly significant error correction term is further proof of the existence of a stable long-term relationship, which is the case here.

Except coefficient of D1LGas (first difference of LGas), all other short run coefficients are significant with positive signs as it is expected.

6- Conclusion

This paper investigates the existence of long-run relation between crude oil, gas and coal prices. The data for us energy market is used in this study. The time period of the analysis extends from October 1983 to October 2008, involving 301 observations. Augmented Dickey-Fuller (ADF) approach

employed for existence of unit root. In brief, Augmented Dickey-Fuller (ADF) tests indicate that Oil and Gas prices are integrated processes of degree one or I(1) and Coal prices is integrated processes of degree five or I(5). As integration degree of variables are not same the Autoregressive Distributed Lag (ARDL) approach to cointegration adapted to cointegration analysis on Oil, Gas and coal prices. The ARDL model was specified in logarithmic form which coefficients mean as elasticities. The model selection fulfilled by Schwarz Bayesian Criterion (SBC) and so ARDL (2, 0, 0) was selected. Moreover, to confirm the stability of the model, CUSUM and CUSUMSQ tests are also conducted with the results that the estimated model is completely stable.

At short run coefficient of D1LGas (first difference of LGas), are statistically insignificant but in long run LGas (logarithm of gas prices) have a significant coefficient. LCoal (logarithm of coal prices) at long run and D1LCoal (first difference of LCoal) at short run have significant coefficients. The results provide that second difference of LOil (D2LOil), indicating short run own price elasticity of oil prices, have a significant coefficient.

The estimated value of EC_{t-1} is -.10198 indicating about 10% speed of adjustment toward equilibrium. It is clear from estimated value of EC_{t-1} that the error correction term (ECM (-1)) has the right sign (negative) and is statistically significant.

Based on the result of cointegration analysis, we can found the long run relationship between oil, gas and coal prices.

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Appendix.1

Unit root tests for variable OIL
The Dickey-Fuller regressions include an intercept but not a trend

297 observations used in the estimation of all ADF regressions.
Sample period from 1984M2 to 2008M10

Test Statistic LL AIC SBC HQC
DF -0.24703 -749.8791 -751.8791 -755.5728 -753.3578
ADF(1) -2.8683 -694.2077 -697.2077 -702.7483 -699.4258
ADF(2) -2.7050 -694.2037 -698.2037 -705.5912 -701.1612
ADF(3) -1.899 -693.1477 -698.1477 -707.3820 -701.8445

95% critical value for the augmented Dickey-Fuller statistic = -2.8714
LL = Maximized log-likelihood AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

Unit root tests for variable OIL
The Dickey-Fuller regressions include an intercept and a linear trend

297 observations used in the estimation of all ADF regressions.
Sample period from 1984M2 to 2008M10

Test Statistic LL AIC SBC HQC
DF -1.6015 -747.4451 -750.4451 -755.9857 -752.6632
ADF(1) -3.7656 -691.2862 -695.2862 -702.6736 -698.2436
ADF(2) -3.6319 -691.2852 -696.2852 -705.5195 -699.9820
ADF(3) -2.9315 -690.3775 -696.3775 -707.4587 -700.8137

95% critical value for the augmented Dickey-Fuller statistic = -3.4264
LL = Maximized log-likelihood AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

Unit root tests for variable GAS
The Dickey-Fuller regressions include an intercept but not a trend

297 observations used in the estimation of all ADF regressions.
Sample period from 1984M2 to 2008M10

Test Statistic LL AIC SBC HQC
DF -1.5054 -182.9664 -184.9664 -188.6602 -186.4452
ADF(1) -1.9937 -178.7620 -181.7620 -187.3026 -183.9801
ADF(2) -1.5382 -175.3503 -179.3503 -186.7378 -182.3078
ADF(3) -1.8087 -174.2769 -179.2769 -188.5112 -182.9737

95% critical value for the augmented Dickey-Fuller statistic = -2.8714
LL = Maximized log-likelihood AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

Unit root tests for variable GAS
The Dickey-Fuller regressions include an intercept and a linear trend

297 observations used in the estimation of all ADF regressions.
Sample period from 1984M2 to 2008M10

Test Statistic LL AIC SBC HQC
DF -3.1691 -179.0640 -182.0640 -187.6046 -184.2821
ADF(1) -3.6957 -173.8772 -177.8772 -185.2647 -180.8347
ADF(2) -3.1914 -171.2459 -176.2459 -185.4802 -179.9427
ADF(3) -3.4902 -169.6975 -175.6975 -186.7787 -180.1337

95% critical value for the augmented Dickey-Fuller statistic = -3.4264
LL = Maximized log-likelihood AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

Unit root tests for variable COAL
The Dickey-Fuller regressions include an intercept but not a trend

297 observations used in the estimation of all ADF regressions.
Sample period from 1984M2 to 2008M10

Test Statistic	LL	AIC	SBC	HQC
DF	3.0999	748.4810	746.4810	742.7873
ADF(1)	2.8249	748.6203	745.6203	740.0797
ADF(2)	2.8203	748.6997	744.6997	737.3122
ADF(3)	2.6287	748.8187	743.8187	734.5844

95% critical value for the augmented Dickey-Fuller statistic = -2.8714
LL = Maximized log-likelihood AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

Unit root tests for variable COAL
The Dickey-Fuller regressions include an intercept and a linear trend

297 observations used in the estimation of all ADF regressions.
Sample period from 1984M2 to 2008M10

Test Statistic	LL	AIC	SBC	HQC
DF	3.2806	760.3759	757.3759	751.8353
ADF(1)	3.4057	760.8059	756.8059	749.4184
ADF(2)	3.9004	762.9563	757.9563	746.7219
ADF(3)	4.0978	763.7465	757.7465	746.6653

95% critical value for the augmented Dickey-Fuller statistic = -3.4264
LL = Maximized log-likelihood AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

Unit root tests for variable D1OIL
The Dickey-Fuller regressions include an intercept but not a trend

285 observations used in the estimation of all ADF regressions.
Sample period from 1985M2 to 2008M10

Test Statistic	LL	AIC	SBC	HQC
DF	-2.9198	-785.4580	-787.4580	-791.1105
ADF(1)	-5.2030	-738.7413	-741.7413	-747.2200
ADF(2)	-5.0599	-738.6684	-746.6684	-749.9733
ADF(3)	-5.4320	-736.8050	-741.8050	-750.9362

95% critical value for the augmented Dickey-Fuller statistic = -2.8718
LL = Maximized log-likelihood AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

Unit root tests for variable D1OIL
The Dickey-Fuller regressions include an intercept and a linear trend

285 observations used in the estimation of all ADF regressions.
Sample period from 1985M2 to 2008M10

Test Statistic	LL	AIC	SBC	HQC
DF	-3.1738	-784.6159	-787.6159	-793.0946
ADF(1)	-5.6448	-736.2291	-740.2291	-747.5341
ADF(2)	-5.5467	-736.0230	-741.0230	-750.1542
ADF(3)	-5.9900	-733.6162	-739.6162	-750.5736

95% critical value for the augmented Dickey-Fuller statistic = -3.4270
LL = Maximized log-likelihood AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

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Unit root tests for variable D1COAL
The Dickey-Fuller regressions include an intercept but not a trend

285 observations used in the estimation of all ADF regressions.
Sample period from 1985M2 to 2008M10

Test Statistic	LL	AIC	SBC	HQC
DF	1.1232	739.2722	737.2722	733.6197
ADF(1)	1.7434	741.8348	738.8348	733.3561
ADF(2)	1.9177	742.1895	738.1895	730.8845
ADF(3)	1.4291	743.4307	738.4307	729.2995

95% critical value for the augmented Dickey-Fuller statistic = -2.8718
LL = Maximized log-likelihood AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

Unit root tests for variable D1COAL
The Dickey-Fuller regressions include an intercept and a linear trend

285 observations used in the estimation of all ADF regressions.
Sample period from 1985M2 to 2008M10

Test Statistic	LL	AIC	SBC	HQC
DF	-.72409	741.4587	738.4587	732.9800
ADF(1)	-.11727	743.5638	739.5638	732.2588
ADF(2)	.079055	743.7695	738.7695	729.6382
ADF(3)	-.34118	745.2621	739.2621	728.3047

95% critical value for the augmented Dickey-Fuller statistic = -3.4270
LL = Maximized log-likelihood AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

Unit root tests for variable D3COAL
The Dickey-Fuller regressions include an intercept but not a trend

261 observations used in the estimation of all ADF regressions.
Sample period from 1987M2 to 2008M10

	Test Statistic	LL	AIC	SBC	HQC
DF	-4.0029	425.6734	423.6734	420.1089	422.2406
ADF(1)	-2.6264	430.7810	427.7810	422.4343	425.6318
ADF(2)	-1.4362	435.7809	431.7809	424.6519	428.9153
ADF(3)	-1.3700	435.7810	430.7810	421.8697	427.1990

95% critical value for the augmented Dickey-Fuller statistic = -2.8727
LL = Maximized log-likelihood AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

Unit root tests for variable D3COAL
The Dickey-Fuller regressions include an intercept and a linear trend

261 observations used in the estimation of all ADF regressions.
Sample period from 1987M2 to 2008M10

	Test Statistic	LL	AIC	SBC	HQC
DF	-4.0726	426.2911	423.2911	417.9443	421.1418
ADF(1)	-2.6925	431.5275	427.5275	420.3985	424.6619
ADF(2)	-1.4883	436.7620	431.7620	422.8507	428.1799
ADF(3)	-1.3893	436.7659	430.7659	420.0724	426.4675

95% critical value for the augmented Dickey-Fuller statistic = -3.4283
LL = Maximized log-likelihood AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

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Unit root tests for variable D2COAL
The Dickey-Fuller regressions include an intercept but not a trend

273 observations used in the estimation of all ADF regressions.
Sample period from 1986M2 to 2008M10

Test Statistic	LL	AIC	SBC	HQC
DF	-2.3969	589.1884	587.1884	583.5790
ADF(1)	-1.2675	593.2946	590.2946	584.8804
ADF(2)	-.52405	595.1762	591.1762	583.9573
ADF(3)	-.88412	596.0268	591.0268	582.0031

95% critical value for the augmented Dickey-Fuller statistic = -2.8722
LL = Maximized log-likelihood AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

Unit root tests for variable D2COAL
The Dickey-Fuller regressions include an intercept and a linear trend

273 observations used in the estimation of all ADF regressions.
Sample period from 1986M2 to 2008M10

Test Statistic	LL	AIC	SBC	HQC
DF	-2.7048	590.3310	587.3310	581.9168
ADF(1)	-1.5834	594.3125	590.3125	583.0935
ADF(2)	-.84381	596.1512	591.1512	582.1275
ADF(3)	-1.1951	597.0454	591.0454	580.2170

95% critical value for the augmented Dickey-Fuller statistic = -3.4276
LL = Maximized log-likelihood AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

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Unit root tests for variable D4COAL
The Dickey-Fuller regressions include an intercept but not a trend
*****
249 observations used in the estimation of all ADF regressions.
Sample period from 1988M2 to 2008M10
*****
Test Statistic   LL      AIC      SBC      HQC
DF      -5.9504  265.3100  263.3100  259.7925  261.8942
ADF(1)   -4.4875  269.0223  266.0223  260.7461  263.8986
ADF(2)   -3.1544  274.6810  270.6810  263.6461  267.8493
ADF(3)   -2.6805  274.7770  269.7770  260.9834  266.2375
*****
95% critical value for the augmented Dickey-Fuller statistic = -2.8732
LL = Maximized log-likelihood    AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion    HQC = Hannan-Quinn Criterion

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Unit root tests for variable D4COAL
The Dickey-Fuller regressions include an intercept and a linear trend
*****
249 observations used in the estimation of all ADF regressions.
Sample period from 1988M2 to 2008M10
*****
Test Statistic   LL      AIC      SBC      HQC
DF      -6.1771  266.7111  263.7111  258.4349  261.5873
ADF(1)   -4.7126  270.2383  266.2383  259.2034  263.4066
ADF(2)   -3.3907  275.8762  270.8762  262.0826  267.3367
ADF(3)   -3.1113  275.9763  269.9763  259.4239  265.7288
*****
95% critical value for the augmented Dickey-Fuller statistic = -3.4291
LL = Maximized log-likelihood    AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion    HQC = Hannan-Quinn Criterion

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Unit root tests for variable DIGAS
The Dickey-Fuller regressions include an intercept but not a trend
*****
285 observations used in the estimation of all ADF regressions.
Sample period from 1985M2 to 2008M10
*****
Test Statistic   LL      AIC      SBC      HQC
DF      -4.8524  -270.8154  -272.8154  -276.4679  -274.2796
ADF(1)   -5.4135  -267.5865  -270.5865  -276.0653  -272.7828
ADF(2)   -4.5124  -265.2954  -269.2954  -276.6004  -272.2238
ADF(3)   -5.3603  -259.6785  -264.6785  -273.8097  -268.3389
*****
95% critical value for the augmented Dickey-Fuller statistic = -2.8718
LL = Maximized log-likelihood    AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion    HQC = Hannan-Quinn Criterion

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Unit root tests for variable DIGAS
The Dickey-Fuller regressions include an intercept and a linear trend
*****
285 observations used in the estimation of all ADF regressions.
Sample period from 1985M2 to 2008M10
*****
Test Statistic   LL      AIC      SBC      HQC
DF      -5.0562  -269.8363  -272.8363  -278.3150  -275.0325
ADF(1)   -5.6607  -266.2848  -270.2848  -277.5098  -273.2132
ADF(2)   -4.7465  -264.2367  -269.2367  -278.3680  -272.8972
ADF(3)   -5.6208  -258.3087  -264.3087  -275.2662  -268.7013
*****
95% critical value for the augmented Dickey-Fuller statistic = -3.4270
LL = Maximized log-likelihood    AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion    HQC = Hannan-Quinn Criterion

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Appendix.2

Unit root tests for variable D5COAL
The Dickey-Fuller regressions include an intercept but not a trend

237 observations used in the estimation of all ADF regressions.
Sample period from 1989M2 to 2008M10

Test Statistic	LL	AIC	SBC	HQC
DF	-7.9277	114.4020	112.4020	108.9340
ADF(1)	-6.3136	115.8504	112.8504	107.6483
ADF(2)	-4.8513	119.7881	115.7881	108.8519
ADF(3)	-4.5798	119.7900	114.7900	106.1199

95% critical value for the augmented Dickey-Fuller statistic = -2.8738
LL = Maximized log-likelihood AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

Unit root tests for variable D5COAL
The Dickey-Fuller regressions include an intercept and a linear trend

237 observations used in the estimation of all ADF regressions.
Sample period from 1989M2 to 2008M10

Test Statistic	LL	AIC	SBC	HQC
DF	-8.0053	115.0015	112.0015	106.7994
ADF(1)	-6.3848	116.3175	112.3175	105.3814
ADF(2)	-4.9127	120.1129	115.1129	106.4428
ADF(3)	-4.6446	120.1133	114.1133	103.7091

95% critical value for the augmented Dickey-Fuller statistic = -3.4300
LL = Maximized log-likelihood AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

Estimated Long Run Coefficients using the ARDL Approach
ARDL(2,0,0) selected based on Schwarz Bayesian Criterion

Dependent variable is LOIL
287 observations used for estimation from 1984M3 to 2008M1

Regressor	Coefficient	Standard Error	T-Ratio[Prob]
LGAS	.38281	.17076	2.2419[.026]
LCOAL	2.0638	.48946	4.2164[.000]
A	1.4930	.18904	7.8976[.000]
T	.0032238	.0010896	2.9587[.003]

Unit root tests for variable RESIDUAL
The Dickey-Fuller regressions include an intercept but not a trend

283 observations used in the estimation of all ADF regressions.
Sample period from 1984M7 to 2008M1

Test Statistic	LL	AIC	SBC	HQC
DF	-15.8592	344.8493	342.8493	339.2039
ADF(1)	-12.8338	346.5386	343.5386	338.0705
ADF(2)	-9.6537	346.9300	342.9300	335.6391
ADF(3)	-8.7120	347.1841	342.1841	333.0705

95% critical value for the augmented Dickey-Fuller statistic = -2.8719
LL = Maximized log-likelihood AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

Unit root tests for variable RESIDUAL
The Dickey-Fuller regressions include an intercept and a linear trend

283 observations used in the estimation of all ADF regressions.
Sample period from 1984M7 to 2008M1

Test Statistic	LL	AIC	SBC	HQC
DF	-15.8326	344.8653	341.8653	336.3971
ADF(1)	-12.8131	346.5577	342.5577	335.2668
ADF(2)	-9.6384	346.9489	341.9489	332.8353
ADF(3)	-8.6978	347.2024	341.2024	330.2660

95% critical value for the augmented Dickey-Fuller statistic = -3.4271
LL = Maximized log-likelihood AIC = Akaike Information Criterion
SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

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Autoregressive Distributed Lag Estimates
ARDL(2,0,0) selected based on Schwarz Bayesian Criterion

Dependent variable is LOIL
287 observations used for estimation from 1984M3 to 2008M1

Regressor	Coefficient	Standard Error	T-Ratio[Prob]
LOIL(-1)	1.3854	.052712	26.2829[.000]
LOIL(-2)	-.48740	.053534	-9.1044[.000]
LGAS	.039038	.021826	1.7886 [.075]
LCOAL	.21046	.061481	3.4231 [.001]
A	.15225	.042502	3.5821 [.000]
T	.3288E-3	.1056E-3	3.1119 [.002]

R-Squared .98078 R-Bar-Squared .98044
S.E. of Regression .072007 F-stat. F(5, 281) 2868.0 [.000]
Mean of Dependent Variable 3.0344 S.D. of Dependent Variable .51485
Residual Sum of Squares 1.4570 Equation Log-likelihood 350.8919
Akaike Info. Criterion 344.8919 Schwarz Bayesian Criterion 333.9134
DW-statistic 1.8840

Diagnostic Tests

* Test Statistics * LM Version * F Version *

* * * * *
* A:Serial Correlation*CHSQ(12)= 12.4026 [.414]*F(12, 269)= 1.0125 [.437]*
* * * * *
* B:Functional Form *CHSQ(1)= 2.5460 [.111]*F(1, 280)= 2.5061 [.115]*
* * * * *
* C:Normality *CHSQ(2)= 111.4867 [.000]* Not applicable *
* * * * *
* D:Heteroscedasticity*CHSQ(1)= .66025 [.416]*F(1, 285)= .65716 [.418]*

A:Lagrange multiplier test of residual serial correlation
B:Ramsey's RESET test using the square of the fitted values
C:Based on a test of skewness and kurtosis of residuals
D:Based on the regression of squared residuals on squared fitted values

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Error Correction Representation for the Selected ARDL Model
ARDL(2,0,0) selected based on Schwarz Bayesian Criterion

Dependent variable is dLOIL
287 observations used for estimation from 1984M3 to 2008M1

Regressor	Coefficient	Standard Error	T-Ratio[Prob]
dLOIL1	.48740	.053534	9.1044[.000]
dLGAS	.039038	.021826	1.7886[.075]
dLCOAL	.21046	.061481	3.4231[.001]
dA	.15225	.042502	3.5821[.000]
dT	.3288E-3	.1056E-3	3.1119[.002]
ecm(-1)	-.10198	.022765	-4.4794[.000]

List of additional temporary variables created:

dLOIL = LOIL-LOIL(-1)
dLOIL1 = LOIL(-1)-LOIL(-2)
dLGAS = LGAS-LGAS(-1)
dLCOAL = LCOAL-LCOAL(-1)
dA = A-A(-1)
dT = T-T(-1)
ecm = LOIL -.38281*LGAS -2.0638*LCOAL -1.4930*A -.0032238*T

R-Squared	.25578	R-Bar-Squared	.24254
S.E. of Regression	.072007	F-stat.	F(5, 281) 19.3156[.000]
Mean of Dependent Variable	.0042028	S.D. of Dependent Variable	.082736
Residual Sum of Squares	1.4570	Equation Log-likelihood	350.8919
Akaike Info. Criterion	344.8919	Schwarz Bayesian Criterion	333.9134
DW-statistic	1.8840		

R-Squared and R-Bar-Squared measures refer to the dependent variable
dLOIL and in cases where the error correction model is highly
restricted, these measures could become negative.